## Egyptian Multiplication

As the Ancient Egyptians did not have a number system based on place value, it was not easy for them to do written calculations. They made a list of products, each one double the previous one, and then selected those needed to give the final product. Keep doubling both columns until 16 is reached. (16 is more than half of 27.) As $27=16+8+2+1$, the ' 4 line' is crossed out. *Add the rest to give $27 \times 41=1107$.

| $28 \times 17$ |  |  |
| :---: | :---: | :---: |
|  |  |  |
| 1 | $\times 17$ | 17 |
| 2 | $\times 17$ | 34 |
| 4 | $\times 17$ |  |
| 8 | $\times 17$ |  |
| 16 | $\times 17$ |  |
| Answer |  |  |


| $35 \times 41$ |  |  |
| :---: | :---: | :---: |
|  |  |  |
| 1 | $\times 41$ | 41 |
| 2 | $\times 41$ | 82 |
| 4 | $\times 41$ |  |
| 8 | $\times 41$ |  |
| 16 | $\times 41$ |  |
| 32 | $\times 41$ |  |
| Answer |  |  |


| $48 \times 32$ |  |  |
| :---: | :---: | :--- |
|  |  |  |
| 1 | $\times 32$ |  |
| 2 | $\times 32$ |  |
| 4 | $\times 32$ |  |
| 8 | $\times 32$ |  |
| 16 | $\times 32$ |  |
| 32 | $\times 32$ |  |
| Answer |  |  |


| $24 \times 22$ |  |  |
| :---: | :---: | :---: |
|  |  |  |
| 1 | $\times 22$ | 22 |
| 2 | $\times 22$ | 44 |
| 4 | $\times 22$ |  |
| 8 | $\times 22$ |  |
| 16 | $\times 22$ |  |
| Answer |  |  |


|  | $59 \times 4$ |
| :---: | :---: |
| 1 | $\times 43$ |
| 2 | x 43 |
| 4 | x 43 |
| 8 | x 43 |
| 16 | x 43 |
| 32 | $\times 43$ |
| Answer |  |


| $55 \times 37$ |  |  |
| :---: | :---: | :--- |
|  |  |  |
| 1 | $\times 37$ |  |
| 2 | $\times 37$ |  |
| 4 | $\times 37$ |  |
| 8 | $\times 37$ |  |
| 16 | $\times 37$ |  |
| 32 | $\times 37$ |  |
| Answer |  |  |

## 'Russian Peasant' Multiplication

The two factors to be multiplied are set down. One is progressively halved with remainders disregarded and the other is progressively doubled until the process cannot continue further.

Delete numbers on the doubled side that are opposite numbers on the halving side that are even. The sum of

| $29 \times 123$ |  |
| :---: | :---: |
| Halve | Double |
| 29 | 123 |
| 14 | 246 |
| 7 | 492 |
| 3 | 984 |
| 1 | 1968 |
| Total |  |
|  | 3567 | the rest gives the correct product. Thus for $29 \times 123$ we have:

Try these using the Russian Peasant method:

| $28 \times 34$ |  |
| :---: | :---: |
| Halve | Double |
| 28 | 34 |
| 14 | 68 |
|  | 136 |
|  |  |
| Total |  |


| $24 \times 43$ |  |
| :---: | :---: |
| Halve | Double |
| 24 | 43 |
| 12 | 86 |
|  |  |
|  |  |
|  |  |
| Total |  |


| $73 \times 69$ |  |
| :---: | :---: |
| Halve | Double |
| 73 | 69 |
|  |  |
|  |  |
|  |  |
| Total |  |


| $31 \times 84$ |  |
| :---: | :---: |
| Halve | Double |
| 31 | 84 |
|  |  |
|  |  |
|  |  |
| Total |  |


| $33 \times 153$ |  |
| :---: | :---: |
| Halve | Double |
|  |  |
|  |  |
|  |  |
|  |  |
| Total |  |


| $64 \times 167$ |  |
| :---: | :---: |
| Halve | Double |
|  |  |
|  |  |
|  |  |
|  |  |
| Total |  |

## Lattice Method

The Lattice, or Gelosia method of multiplication (so called because the setting out of the algorithm resembled the grate, or lattice, placed on windows at the time) was used in Europe from the $15^{\text {th }}$ century onwards.

To multiply $92 \times 45$, you would draw a grid (or lattice) two cells across and two cells down.

The numbers to be multiplied are written across the top and side of the grid.


92


4

5
92


4


The units digit is placed in the bottom. The top may be left blank.
The results of multiplying $92 \times 45$ are then recorded. The answer is found by adding diagonally, beginning at the lower right.


## Product Puzzles

Put the numbers 1, 2, 3, 4 and 5 in the boxes below and make the:

largest product $\qquad$
smallest product $\qquad$

Now try these numbers:


- Look for a pattern for producing the largest product and the smallest product. Describe the pattern.

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