

Accessing mathematical content through the Proficiency Strands - Years 4 - 9



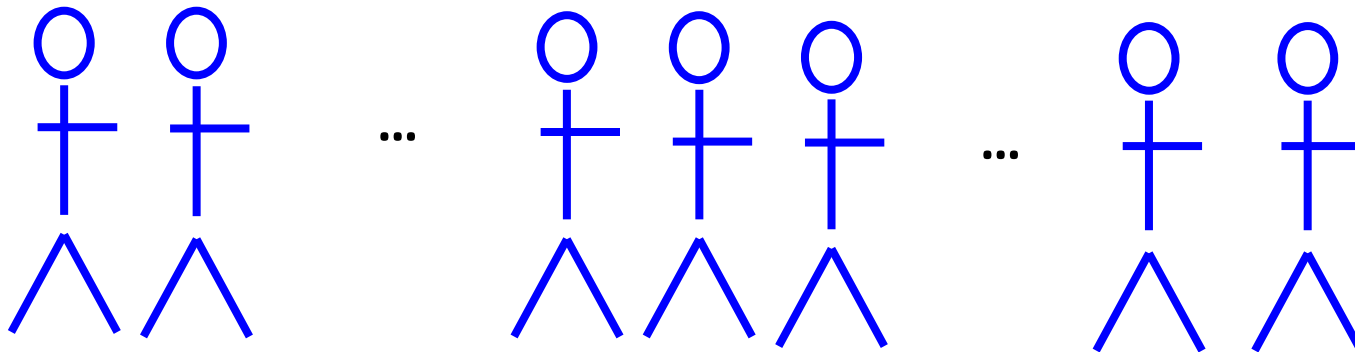
Lorraine Day & Derek Hurrell



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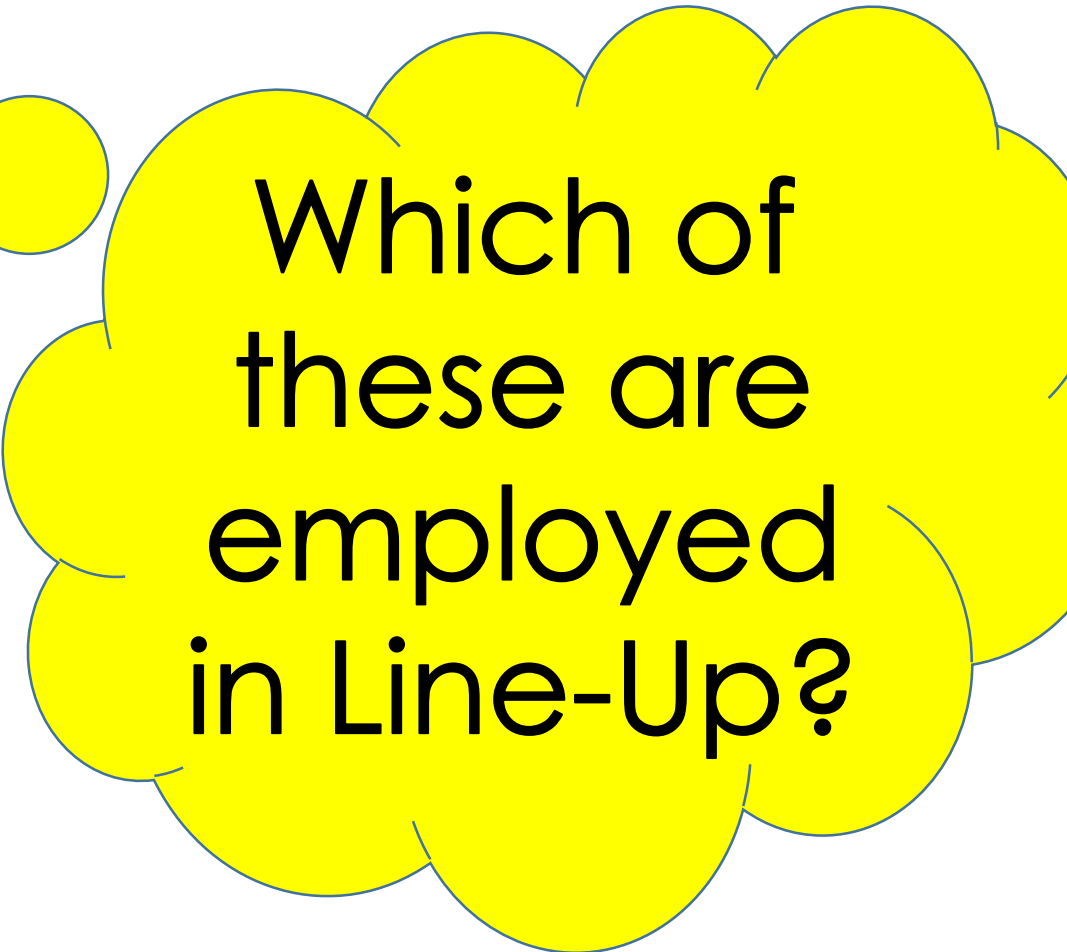
Line-up!

**I am 19th from either end.
How many in the line?**

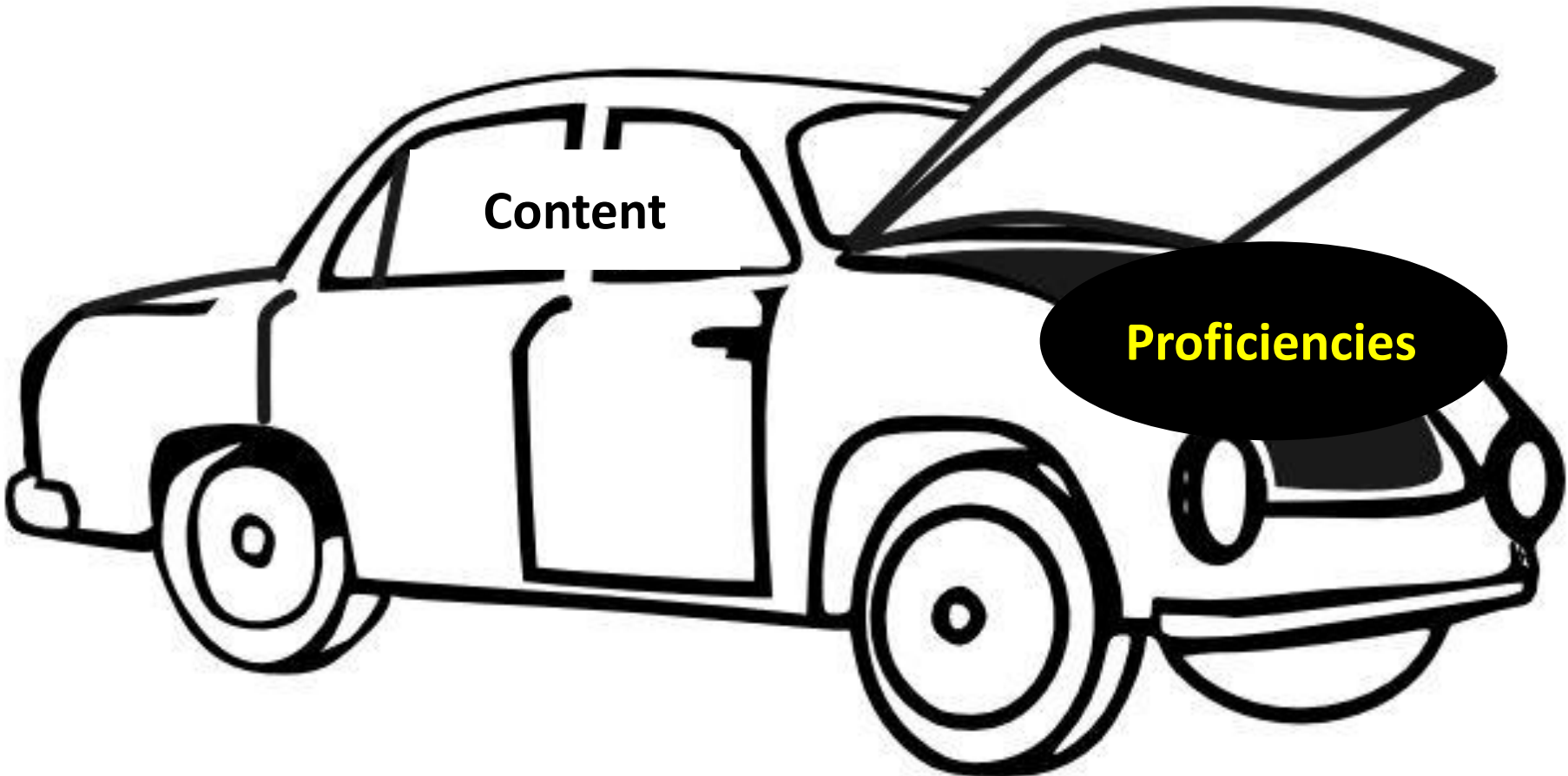


Proficiency Strands

- Understanding
- Fluency
- Problem Solving
- Reasoning



Which of these are employed in Line-Up?



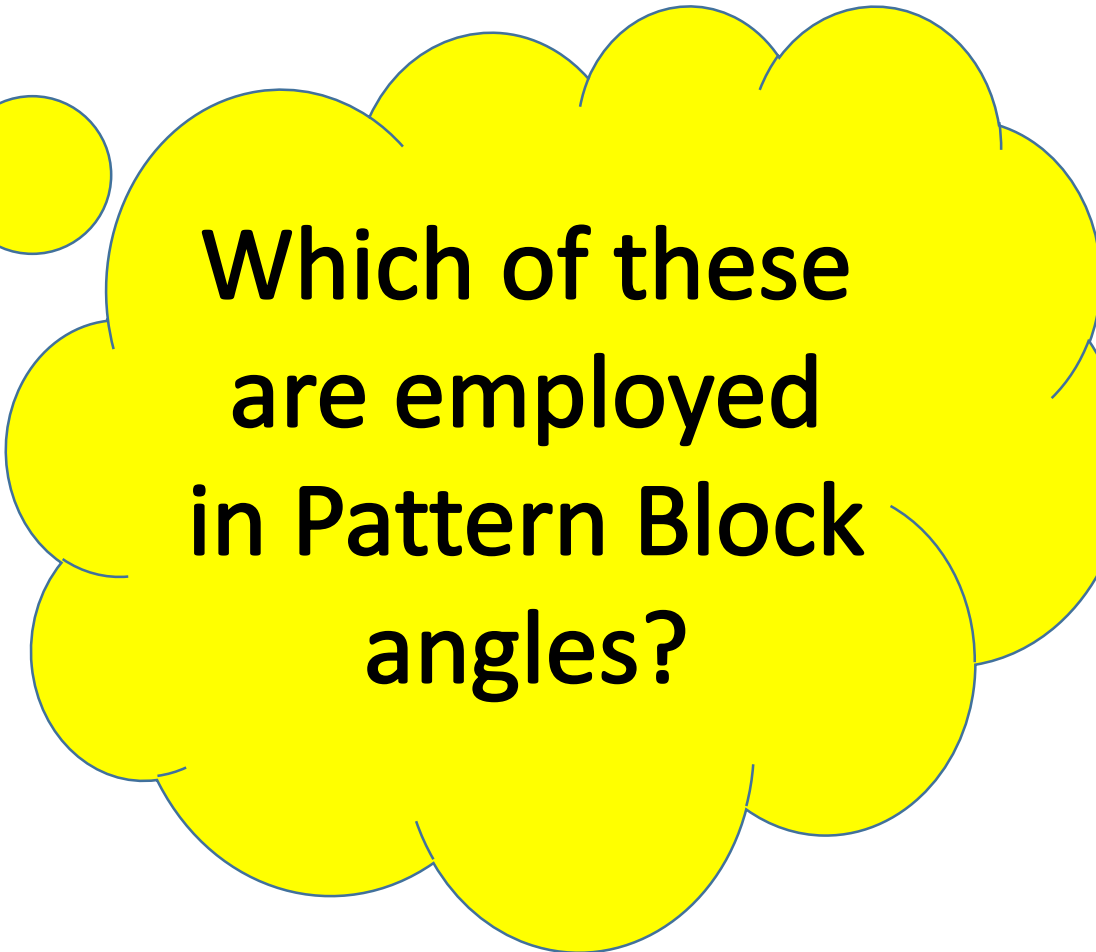
Proficiencies: The power behind
the curriculum

Without using a protractor,
how many degrees is each
angle in the different
Pattern Blocks?

How can you prove your
answers are correct?

Proficiency Strands

- Understanding
- Fluency
- Problem Solving
- Reasoning



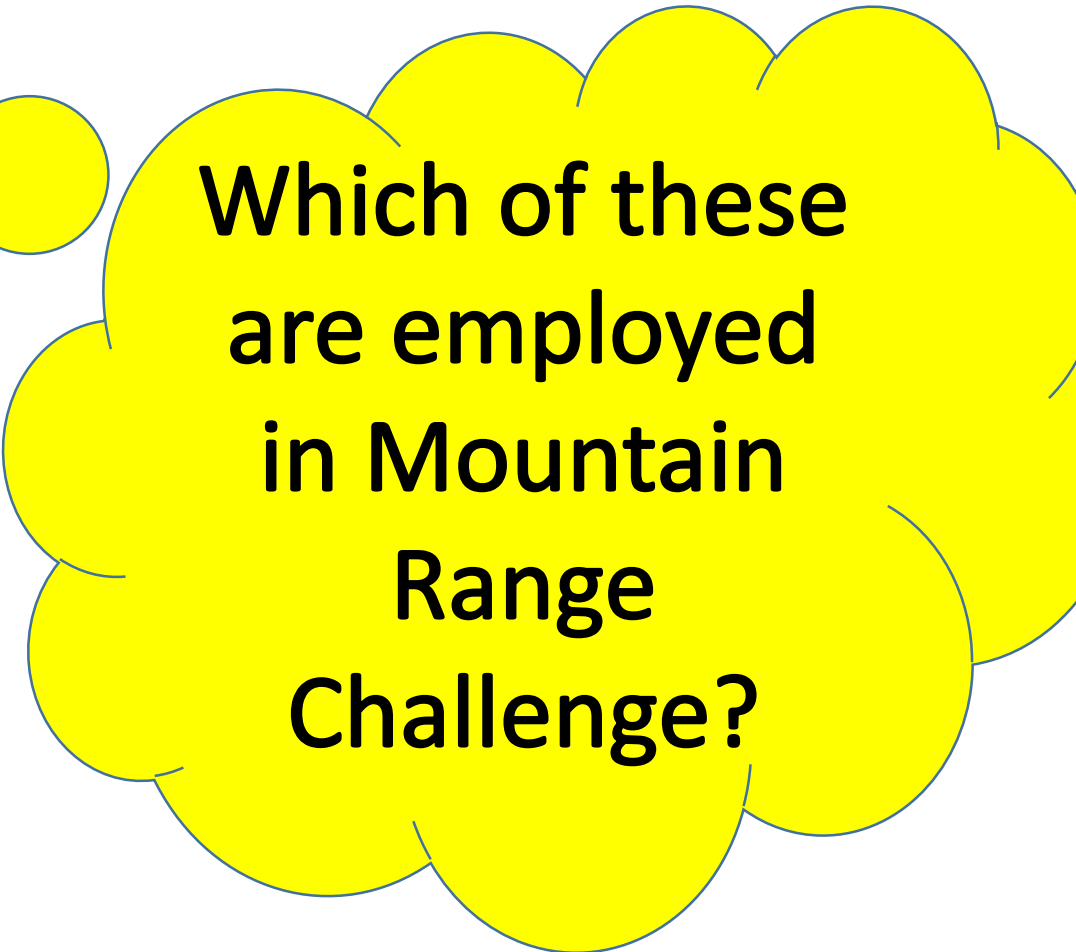
**Which of these
are employed
in Pattern Block
angles?**

Mountain Range Challenge



Proficiency Strands

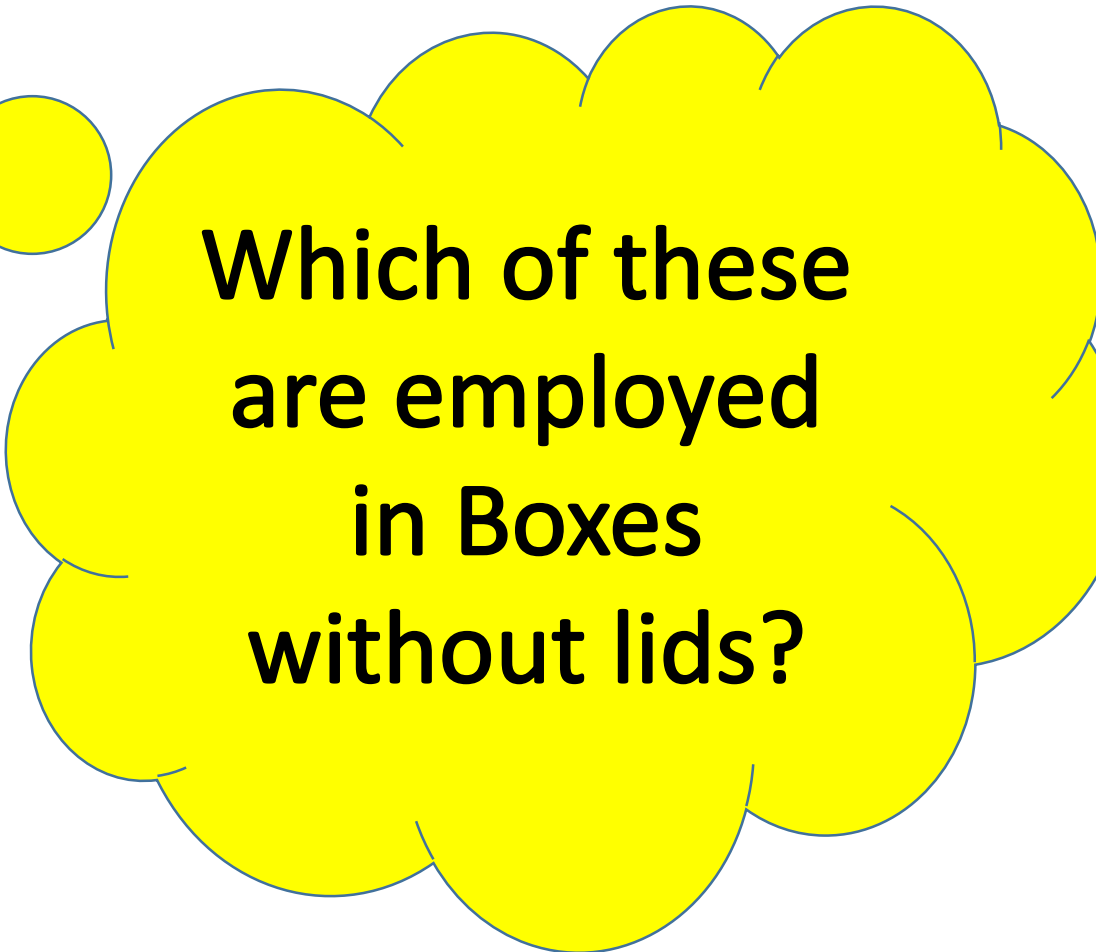
- Understanding
- Fluency
- Problem Solving
- Reasoning



**Which of these
are employed
in Mountain
Range
Challenge?**

Proficiency Strands

- Understanding
- Fluency
- Problem Solving
- Reasoning



**Which of these
are employed
in Boxes
without lids?**

Proficiency Strands

The proficiency strands... describe **how content is explored or developed**, that is, the **thinking and doing** of mathematics. They provide the language to build in the developmental aspects of the learning of mathematics and have been incorporated into the content descriptions of the three content strands. This approach has been adopted **to ensure students' proficiency in mathematical skills develops** throughout the curriculum and becomes increasingly sophisticated over the years of schooling.

Understanding

Students build a robust knowledge of adaptable and transferable mathematical concepts. They make connections between related concepts and progressively **apply** the familiar to develop new ideas. They **develop** an understanding of the relationship between the **'why'** and the **'how'** of mathematics. Students **build** understanding when they **connect** related ideas, when they **represent** concepts in different ways, when they **identify** commonalities and differences between aspects of content, when they **describe** their thinking mathematically and when they **interpret** mathematical information.



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**NO rules without
meaning!
(the why and the how!)**



Fluency



Students develop skills in **choosing** appropriate procedures, carrying out procedures **flexibly**, **accurately**, **efficiently** and **appropriately**, and recalling **factual** knowledge and **concepts** readily. Students are fluent when they calculate answers efficiently, when they recognise robust ways of answering questions, when they choose appropriate methods and **approximations**, when they **recall** definitions and regularly **use** facts, and when they can **manipulate** expressions and equations to find solutions.

Fluency



Students develop skills in choosing appropriate procedures, carrying out procedures flexibly, accurately, efficiently and appropriately, and recalling factual knowledge and concepts readily. Students are fluent when they calculate answers efficiently, when they recognise robust ways of answering questions, when they choose appropriate methods and approximations, when they recall definitions and regularly use facts, and when they can manipulate expressions and equations to find solutions.

Choose and use
the right tools
correctly

Problem Solving

Students develop the ability to make choices, interpret, formulate, **model** and **investigate** problem situations, and **communicate** solutions effectively. Students **formulate** and **solve** problems when they use mathematics to represent unfamiliar or meaningful situations, when they **design** investigations and **plan** their approaches, when they **apply** their existing strategies to **seek** solutions, and when they **verify** that their answers are reasonable.



CALM DOWN

Problem Solving

Students develop the ability to make choices, interpret, formulate, model and investigate problem situations and communicate solutions effectively. Students formulate and solve problems when they use mathematics to represent unfamiliar or meaningful situations, when they design investigations and plan their approaches, when they apply their existing strategies to seek solutions, and when they verify that their answers are reasonable.

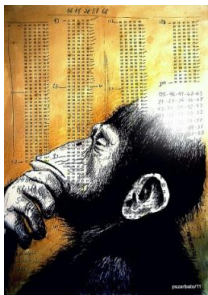
Involves investigating, thinking, and communicating.
(The creative element of mathematics!)



CALM DOWN

Reasoning

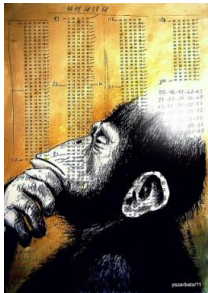
Students develop an increasingly sophisticated capacity for logical thought and actions, such as **analysing**, **proving**, **evaluating**, **explaining**, **inferring**, **justifying** and **generalising**. Students are reasoning mathematically when they **explain** their thinking, when they **deduce** and **justify** strategies used and conclusions reached, when they **adapt** the known to the unknown, when they **transfer** learning from one context to another, when they **prove** that something is true or false and when they **compare** and **contrast** related ideas and explain their choices.



Reasoning

Students develop an increasingly sophisticated capacity for logical thought and actions, such as **analysing**, **proving**, **evaluating**, **explaining**, **inferring**, **justifying** and **generalising**. Students are reasoning mathematically when they **explain** their thinking, when they **deduce** and **justify** strategies used and conclusions reached, when they **adapt** the known to the unknown, when they **transfer** learning from one context to another, when they **prove** that something is true or false and when they **compare** and **contrast** related ideas and explain their choices.

**Explain thinking
and justify
decisions
(Convince me!)**



- If we are seeking **fluency**, then clear explanations followed by practice will work
- If we are seeking **understanding**, then very clear and interactive communication between teacher and students and between students will be necessary
- If we want to foster **problem solving** and **reasoning**, then we need to use tasks with which students can engage, which require them to make decisions and explain their thinking

Mathematically Rich Tasks

- Allow students to work mathematically and see others working mathematically to **solve problems**
- Easy to start while still providing opportunities for challenge and extension
- Situated within meaningful or intriguing contexts
- Develop thinking, **reasoning** and **communicating** skills
- Seek genuine **understandings**
- Cater for a variety of learning styles
- Encourage students to **explain their thinking**
- Develop **fluency** in context

Thank you!

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